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Fractions IIB

*Part Two of the
Four Operations with Fractions*

Multiplication and Division

With

Simple and Mixed Fractions

Levels I-V

*(Including Full Synthesis of the Four Operations
with Simple and Mixed Fractions)*

Worksheet Masters & Answer Keys

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The design and intent of the following TEACHER GUIDED pages are to provide students with specific pre-support in making key connections for each respective content area. Therefore, the TEACHER GUIDED pages are to be done with the students to ensure students are structured and prepared for the problem sets following each TEACHER GUIDED page(s). Consequently, the TEACHER GUIDED pages should never be assigned as independent work.

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