Fractions IIB

Part Two of the
Four Operations with Fractions

Multiplication and Division
With
Simple and Mixed Fractions
Levels I-V
(Including Full Synthesis of the Four Operations
with Simple and Mixed Fractions)

Worksheet Masters & Answer Keys

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